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Reliability-based robust design of smart sensing systems for failure diagnostics using piezoelectric materials

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ABSTRACT

This paper presents a reliability-based robust design approach to develop piezoelectric materials based structural sensing systems for failure diagnostics and prognostics. A detectability measure is defined to evaluate the performance of any given sensing system, and the sensing system design problem can be formulated to maximize detectability for different failure modes by optimally allocating piezoelectric materials into a target structure. This formulation can be conveniently solved within a reliability-based robust design framework to ensure design robustness while considering the uncertainties such as those from structure properties and operation conditions. Two case studies, that design sensor networks for an aircraft wing panel and a power transformer structure, are employed to demonstrate the effectiveness of the proposed methodology in developing multifunctional material sensing systems.

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1. Introduction

With a growing complexity of engineered systems, failure diagnostics techniques have been prevalently employed to prevent potential catastrophic failures and improve system reliability and safety. Real-time health diagnostics interpret data acquired by smart sensors, and utilize these data streams in making critical operation and maintenance decisions [1]. Enormous benefits can be provided by effective health diagnostics activities, such as improved system safety, reliability, and reduced costs for the operation and maintenance of complex engineered systems. Structure maintenance and life-cycle management is an area that can significantly benefit from diagnostics and improved maintenance practices, as unexpected system breakdowns could be prohibitively expensive [2]. Thus to reduce and possibly eliminate such problems, it is important to accurately assess the health condition of an operating system in real time through effective health diagnostics. Researches on condition monitoring address these challenges by assessing system health states utilizing sensory information from the functioning system [3–5]. Monitoring of system health state (HS) changes over time provides valuable information about the performance degradation of system

components for critical maintenance decision makings, and has been successfully applied to many engineering systems such as bearings [6–9], machine tools [10], power transformers [11], engines [12], aircraft wings [13], and turbines [14]. In the literature, there are two categories of approaches in general that are often employed for health diagnostics, machine learning techniques and statistical inference techniques. The machine learning-based health diagnostics approaches can further be divided into supervised learning, unsupervised learning and semi-supervised learning techniques. In addition to the aforementioned machine learning-based algorithms, statistical inference-based algorithms can also be used to classify system HSs based on statistical distances such as Mahalanobis distance [15], k-nearest neighbor method [16] and k-mean clustering [17]. Significant advancements in diagnostics area have been achieved by applying classification techniques based on machine learning or statistical inferences, resulting in a number of classification methods, such as back-propagation neural networks [18–21], deep belief networks [22,23], support vector machines [24–28], self-organizing maps [29], and Mahalanobis distance (MD) [15]. Some researchers combined two or more existing techniques to form hybrid models to achieve better diagnostic performance. Zhang et al. [9] proposed a bearing fault diagnosis methodology using multi-scale entropy (MSE) and adaptive neuro-fuzzy inference system. Saimurugan et al. [24] presented a multi-component fault diagnosis of a rotational mechanical system based on decision trees and support vector machines.

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Nomenclature

R	reliability	$f_x(x)$	probability density function
Φ	standard Gaussian cumulative distribution function	$f_{(\cdot \cdot)}$	conditional probability density function or likelihood function
β_t	target reliability index	p_{fs}	probability of system failure
C_L	user-defined confidence level	G_i	function of the i th constraint
$F(x)$	cumulative distribution function	C	cost function
$F^{-1}(x)$	inverse cumulative distribution function		

Despite a variety of numerical diagnostics algorithms being developed and a broad range of successful applications in various engineering fields being reported in the literature, one of the key challenges in structural health diagnostics lies in the fact that health relevant sensory data must be collected effectively so that enough evidences can be provided for diagnostics algorithms to conduct health state identification and damage detection. However, implicit relationship between sensory signals and system health states as well as sensor noise and uncertainties related to system operating conditions render a grand challenge in developing an effective sensor network so that system health states can be accordingly diagnosed accurately with sensory data collected from the sensor network. To overcome this challenge, a sensor network must be developed with sensors nodes being optimally placed so that the differences between different system health states can be reflected clearly on sensory signals. In addition, the sensor network must be designed to ensure the robustness of health diagnostics given the aforementioned uncertainties and variability involved in sensing and diagnosing processes. In the literature, sensor placement optimization under uncertainties has been studied for structural health monitoring applications [30,31], and further optimal location of sensors has been presented for parametric identification of linear structural systems [32]. A methodology for optimally locating sensors in a dynamic system [33,34] was developed as a probabilistic approach in structural health monitoring system. The study in [35] developed a Bayesian approach to optimize sensor placement for structural health monitoring. In [36], an optimal sensor location methodology for structural identification and damage detection has been studied. Most of these methods were settled for allocating a number of sensors to distinguish a specific health state of structural damage, and their applications were limited by the type of health state failure mechanisms. Although reported studies on sensor placement optimization have showed improvements on health diagnostics performance, there are two fundamental challenges that hinder the broad applications of this technique. First, the sensing capability of the sensor nodes used in sensor placement studies have been mostly assumed to be independent to the target systems, which is generally not true for practical structural applications; Second, there is no quantitative measure for the diagnostics performance related based upon a given sensor network design, thus, the performance robustness cannot be ensured in the sensor network design process.

To address the aforementioned sensor network design challenges for structural diagnostics applications, this paper presents a novel reliability-based robust design optimization (RBRDO) framework for structural sensing function design using multifunctional materials. The RBRDO technique has been developed to ensure the performance robustness thus improve quality and reliability in product and process design, while considering uncertainties involved in different stages of a system's life cycle [37–42]. In detail, design optimization of piezoelectric embedded sensor patches is considered to realize structural sensing function [43–48]. First, a generic detectability measure is defined in this study to quantify the performance of a given sensing system for

diagnostics under uncertainty. A novel detectability analysis approach based on Mahalanobis distance classifier is then developed to carry out the detectability analysis for a given sensing system design. Second, with the defined detectability measure and developed detectability analysis approach, a novel reliability-based robust design optimization (RBRDO) framework is presented for sensing system design in order to minimize the system development costs while maintaining the predefined detectability target. The rest of the paper is organized as follows. First, smart sensing with piezoelectric materials is introduced in Section 2. In Section 3, a detectability measure is defined in a probabilistic form as a unified quantitative measure for the performance of any given sensing system used for the structural health diagnostics. A general approach for detectability evaluation is also introduced based on health state classification. In Section 4, a generic RBRDO framework is developed to design smart material systems for the structural health diagnostics and prognostics. Two case studies are used in Section 5 to demonstrate the effectiveness of the proposed methodology in developing structural sensing systems.

2. Smart sensing with piezoelectric materials

Piezoelectric materials can be potentially applied in both sensing and actuating applications [49–53]. In sensing applications the PZT sensor is attached to a structure and exposed to a stress field that creates electric charges (direct piezoelectric effect). In actuating applications the PZT actuator is attached to a structure and an external electric source is applied to the actuator that induce strain field (reverse piezoelectric effect). In both cases the constitutive relationship can be mathematically formulated as follows:

$$\varepsilon_i = S_{ij}^E \sigma_j + d_{mi} E_m \tag{1}$$

$$D_m = d_{mi} \sigma_i + e_{ik}^D E_k \tag{2}$$

where the indexes $i, j = 1, 2, \dots, 6$ and $m, k = 1, 2, 3$ refer to different directions within the material coordinate system [51], σ is a vector of the stress (N/m²) and ε is a vector of the strain, d is a matrix of the piezoelectric strain constants that defines strain per unit at constant stress (m/V), E is a vector of the electric field (V/m), S^E is a matrix of the elastic compliance (m²/N), D is a vector of the electric

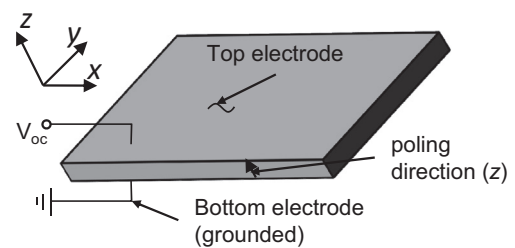


Fig. 1. Schematic of a piezoelectric ceramic sheet.

displacement (Coulomb/m²), e^{σ} is a matrix of the dielectric permittivity (F/m). This paper considers a sensing application which utilizes d_{31} effect of PZT material: a voltage output along the thickness direction as a response of in-plane strain (see Fig. 1).

This paper considers use of piezoelectric materials for real-time monitoring of structural damages utilizing direct piezoelectric effect – generation of electric potential in response to an applied mechanical stress. A harmonic vibration with a fixed frequency is assumed for a structure to be monitored. Harmonic response analysis solves the time-dependent equation of motion for linear structures under steady-state vibration with a fixed excitation frequency. Considering a general equation of motion for a piezoelectric coupled-field structure after the application of the variational principle and finite element (FE) discretization, the coupled FE matrix equation is derived as [54]:

$$\begin{bmatrix} \mathbf{M} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{Bmatrix} \ddot{\mathbf{u}} \\ \ddot{\mathbf{V}} \end{Bmatrix} + \begin{bmatrix} \mathbf{C} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{Bmatrix} \dot{\mathbf{u}} \\ \dot{\mathbf{V}} \end{Bmatrix} + \begin{bmatrix} \mathbf{K} & \mathbf{K}^z \\ (\mathbf{K}^z)^T & \mathbf{K}^d \end{bmatrix} \begin{Bmatrix} \mathbf{u} \\ \mathbf{V} \end{Bmatrix} = \begin{Bmatrix} \mathbf{F} \\ \mathbf{L} \end{Bmatrix} \quad (3)$$

where \mathbf{M} , \mathbf{C} , and \mathbf{K} are the structural mass, damping, and stiffness matrices respectively, \mathbf{K}^z is piezoelectric coupling matrix, \mathbf{K}^d is dielectric conductivity matrix, $\{\mathbf{u}\}$ is displacement vector, $\{\mathbf{V}\}$ is voltage vector, and $\{\mathbf{F}\}$ and $\{\mathbf{L}\}$ are structural and electrical load vectors. The electrical load vector $\{\mathbf{L}\}$ is assumed to be zero in this paper, thus, only the structural input loading exists for the design of structural sensing functions. Although the application problems with piezoelectric material patches could have very little effect on the structure stiffness, however, it could still affect the PZT sensor outputs. Thus, in the presented sensor network design study, the coupling effects have been taken into consideration, as shown in Eq. (3), in which \mathbf{K}^z indicates piezoelectric coupling matrix. In the harmonic response analysis, all points in the structure are vibrating at a same known frequency. Therefore displacements and voltage can be defined as:

$$\begin{aligned} \{\mathbf{u}\} &= \{\mathbf{u}_{\max}\} e^{j(\varphi + \omega t)} = \{\mathbf{u}_{\max}(\cos \varphi + j \sin \varphi)\} e^{j\omega t} = [\{u_{re}\} + j\{u_{im}\}] e^{j\omega t} \\ \{\mathbf{V}\} &= \{\mathbf{V}_{\max}\} e^{j(\varphi + \omega t)} = \{\mathbf{V}_{\max}(\cos \varphi + j \sin \varphi)\} e^{j\omega t} = [\{V_{re}\} + j\{V_{im}\}] e^{j\omega t} \end{aligned} \quad (4)$$

where $\{\mathbf{u}_{\max}\}$ and $\{\mathbf{V}_{\max}\}$ are the maximum displacement and voltage, respectively; φ is the phase angle, ω is the imposed excitation frequency, j is the square root of -1 , and the sub-indices re and im represent the real and imaginary components, respectively. The force vector can be specified analogously as follows:

$$\{\mathbf{F}\} = \{\mathbf{F}_{\max}\} e^{j(\varphi + \omega t)} = \{\mathbf{F}_{\max}(\cos \varphi + j \sin \varphi)\} e^{j\omega t} = [\{F_{re}\} + j\{F_{im}\}] e^{j\omega t} \quad (5)$$

Finally, substituting Eqs. (4) and (5) into Eq. (3) and canceling the $e^{j\omega t}$ term, the following structural equations [54] can be obtained

$$\left(-\omega^2 \begin{bmatrix} \mathbf{M} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} + j\omega \begin{bmatrix} \mathbf{C} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} + \begin{bmatrix} \mathbf{K} & \mathbf{K}^z \\ (\mathbf{K}^z)^T & \mathbf{K}^d \end{bmatrix} \right) \begin{Bmatrix} \{u_{re}\} + j\{u_{im}\} \\ \{V_{re}\} + j\{V_{im}\} \end{Bmatrix} = \begin{Bmatrix} \{F_{re}\} + j\{F_{im}\} \\ \mathbf{0} \end{Bmatrix} \quad (6)$$

One of the commonly used piezoelectric materials is lead zirconate titanate (PZT), a piezoelectric ceramic, which has wide application in vibration sensors and health monitoring systems [46]: a self-sensing piezoelectric actuator for collocated control [47], health monitoring/damage detection of a rotorcraft planetary gear train system using piezoelectric sensors [48], and smart sensor system for structural condition monitoring of wind turbines [49]. In this paper a new smart sensing system design framework will be developed for structural health diagnostics using piezoelectric materials.

3. Probabilistic detectability measure for diagnostics

Sensing systems can monitor the physical behaviors and determine the health state of a system. However, false alarm may occur due to the uncertainties of system operation processes

and manufacturing. Therefore, the performance of sensing system should be qualified using a probabilistic method, so that the accurate detection of system health states can be achieved. In the proposed RBRDO framework, a set of health states must be categorized based on historical failure data. Thus correct and incorrect detection rates of every health state can be defined as the sensing performance measures. The correct detection rate can be calculated by a conditional probability that the sensing system can correctly detect the health state given that the system is operated at one health state. In contrast, the incorrect detection rate can be expressed as a conditional probability that the sensing system detects wrong information. Using the data of correct and incorrect detection rates, the sensing system detectability can be expressed by constructing a probability-of-detection (PoD) matrix.

This section introduces the concept of detectability and the method to evaluate the detectability for each health state based on structural simulation and system health state classification. Section 3.1 introduces the concept of probability of detection matrix to qualify the sensing system. Section 3.2 presents the Mahalanobis distance based approach for health state classification. In this research, it is assumed that all numerical models are valid and they deliver accurate results associated with actual systems.

3.1. Probability-of-detection (PoD) matrix

A PoD matrix defines the overall sensing system diagnostics performances, which consists of the probabilities of correct detection and misdetection for all predefined health states. A general form of the PoD matrix is shown as

$$\text{PoD} = \begin{bmatrix} P_{11} & P_{12} & P_{13} & \cdots & P_{1N_{HS}} \\ P_{21} & P_{22} & P_{23} & \cdots & P_{2N_{HS}} \\ P_{31} & P_{32} & P_{33} & \cdots & P_{3N_{HS}} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ P_{N_{HS}1} & P_{N_{HS}2} & P_{N_{HS}3} & \vdots & P_{N_{HS}N_{HS}} \end{bmatrix} \quad (7)$$

In the PoD matrix, N_{HS} represents the number of health states (HS), where P_{ij} indicates the probabilistic relationship between the true system health state, i , and the health state, j , detected by the sensing system. P_{ij} can be defined as the conditional probability that the system is detected to be operated at HS_j by the sensing system given that the system is operated at HS_i . This relationship can be statistically expressed as

$$P_{ij} = \Pr(HS_j \text{ as Detected} | HS_i \text{ as True}) \quad (8)$$

To provide a probabilistic measure for diagnostics performance of a sensing system while considering uncertainties induced in manufacturing and system operating processes, detectability can be defined for each system health state accordingly based on the diagonal terms in the PoD matrix. As an example, the detectability for the i th system health state (HS_i) can be statistically defined below as

$$D_i = P_{ii} = \Pr(HS_i \text{ as Detected} | HS_i \text{ as True}) \quad (9)$$

While considering all health states, the diagonal terms in the PoD matrix, which represent the probabilities of correct detection for predefined health states, will determine the overall SN detection performance. With the predefined detectability requirements, these diagonal terms in the PoD matrix will then constitute N_{HS} number detectability targets to be satisfied during the sensing function design process. In the following, an example is employed to demonstrate the proposed detectability measure.

Suppose that only one sensor is used to collect data for diagnostics and three predefined health states are given as following: (1) Health State 1 (HS_1): the system is operating normally without any damage and sensor output follows a normal distribution as $N(1, 0.9^2)$; (2) Health State 2 (HS_2): the system is operating but has some minor damage that follows a normal distribution as $N(3, 0.6^2)$ and (3) Health State 3 (HS_3): The system is operating but has a severe damage that follows a normal distribution as $N(6, 1.5^2)$. In what follows, the detectability values for all three defined health states will be determined based on the available information. To calculate the detectability value for each health state, it is necessary to classify any given set of testing sensory data into one of the three health states. This can be accomplished simply by defining a normalized distance, the z-score for this example, between the testing data and the sensor output distribution for each health state. The normalized distance measures the divergence of the testing data from the sensor output distribution of each health state, and consequently the testing data should be classified into the health state which has the smallest normalized distance.

To facilitate the diagnostics process, boundaries between two health states will be identified by one neutral point that leads to three equal normalized distances as shown in Fig. 2. The natural point (X_{1-2}) between HS_1 and HS_2 can be calculated using Eq. (10), and the natural point (X_{2-3}) between HS_2 and HS_3 can be also calculated accordingly as shown in Eq. (11).

$$\frac{X_{1-2} - 1}{0.9} = \frac{3 - X_{1-2}}{0.6}, \quad X_{1-2} = 2.2000 \quad (10)$$

$$\frac{X_{2-3} - 3}{0.6} = \frac{6 - X_{2-3}}{1.5}, \quad X_{2-3} = 3.8571 \quad (11)$$

With the identified neutral points between different health states, the detectability (D_i) can be evaluated as shown in Eqs. 12–14, respectively, using the conditional probability defined in Eq. (9).

$$D_1 = P_{11} = \Pr(\text{Detected as } HS_1 | \text{System is at } HS_1) = \Pr(X \leq X_{1-2} | X \sim N(1, 0.9^2)) = 0.9088 \quad (12)$$

$$D_2 = P_{22} = \Pr(\text{Detected as } HS_2 | \text{System is at } HS_2) = \Pr(X_{1-2} \leq X \leq X_{2-3} | X \sim N(3, 0.6^2)) = 0.8322 \quad (13)$$

$$D_3 = P_{33} = \Pr(\text{Detected as } HS_3 | \text{System is at } HS_3) = \Pr(X \geq X_{2-3} | X \sim N(6, 1.5^2)) = 0.9234 \quad (14)$$

From this mathematical example with analytical evaluation of the detectability, it is clear that statistical distributions and health

states classification of sensor outputs are critical for detectability analysis of a given sensing system. Nevertheless, in practical engineering applications, a sensing system will generally contain numerous sensors to deal with much more than three health states. Thus, analytical evaluation of sensing system detectability becomes challenging, for example, the calculation of boundaries between different health states. In addition, statistical distributions of sensors' outputs for all health states are not commonly available. To effectively evaluate the detectability for a given sensing system design, a new detectability analysis approach is developed in this study, as detailed in the next subsection, in which the Mahalanobis distance (MD) classifier is employed to handle the uncertainties of sensor output for each system health state and classify sensory data points for detectability calculation.

3.2. Detectability analysis using Mahalanobis distance classifier

This section details a detectability analysis method, which employs Mahalanobis distance (MD) classifiers for the calculation of detectability values based on structural simulation and system health state classification. A MD classifier quantitatively measures the similarity between an online data point and different training data sets from different system health states, and represents the similarity using a Mahalanobis distance measure, whereby a shorter distance indicates a greater similarity. With the MD measure, a testing data point will can be accordingly classified into a health state that induces a minimum Mahalanobis distance value by its training data set. Thus, a MD classifier is capable of categorizing a testing data point measured from an operating system by a sensor network to a predefined system health state from which the sensory data point is most likely measured. Mathematically, the Mahalanobis distance [55] of a testing data point from the training data sets of a health state can be calculated by

$$MD_i = \sqrt{(X - M_i)^T \Sigma_i^{-1} (X - M_i)} \quad (15)$$

where the T denotes matrix transpose, X is the given testing data point to be classified, M_i and Σ_i represent the mean vector and the covariance matrix, respectively, for the training data sets for the i th health state, HS_i .

In the following, one example is used to explain the MD-based health state classification process for detectability analysis. In this example, there are two sensors and three predefined health states ($N_{HS} = 3$), in which HS_1 is used for system healthy, HS_2 for system with minor damage, and HS_3 for system with severe damage. The training data information from two different sensors corresponding to different health states is listed in Table 1. In this example, for each health state 100 sensory data points are generated from the distribution information as shown in Table 1, and used as the training data sets.

First, to demonstrate the MD-based classification process, five testing data points, as shown in the first two columns in Table 2, will be classified to its corresponding health states. Using the MD classifier, the MD values for each testing data set can be calculated with the training data sets using Eq. (15), and a testing data point is classified to a given health state that provides the minimum MD values out of all three. For example, to classify the first testing data point [2.07, 0.78] as shown in Table 2, the MD values are calculated

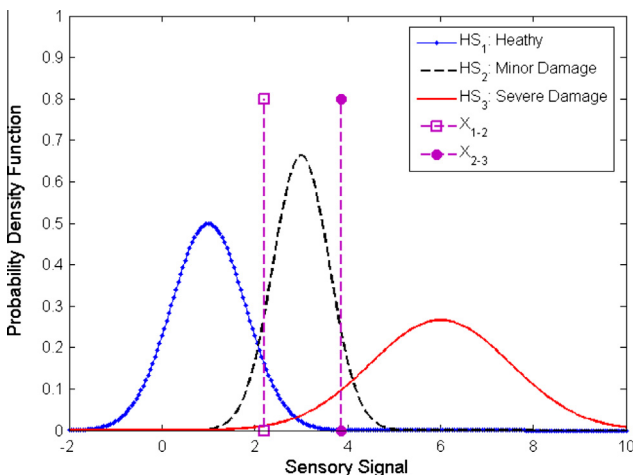


Fig. 2. Sensor output distributions neural points.

Table 1
Predefined system health states.

Health state	Sensor 1	Sensor 2
HS_1	$N(1.5, 0.5^2)$	$N(1.5, 0.5^2)$
HS_2	$N(1.5, 0.5^2)$	$N(1.5, 0.5^2)$
HS_3	$N(1.5, 0.5^2)$	$N(1.5, 0.5^2)$

Table 2
Health states classification using MD classifier.

Testing data		Mahalanobis distance			Classified state
S_1	S_2	HS_1	HS_2	HS_3	
2.07	0.78	4.83	73.79	27.52	HS_1
0.89	-0.88	5.19	48.61	2.72	HS_3
1.72	0.46	1.43	62.19	17.57	HS_1
-2.54	0.90	90.97	1.13	34.76	HS_2
0.58	-1.14	10.12	44.93	2.13	HS_3

to be 4.83, 73.79, and 27.52 using the training data sets from three different health states, respectively, and consequently this testing data point will be classified as it belongs to HS_1 since the MD value 4.83 obtained from the first health state is the minimum.

In the following, the PoD matrix for this example will be evaluated and the detectability values for all three predefined health states will be determined by following the same procedure used above. Suppose that there are totally T_i sets (here $T_i = 100$ is used) of testing data from the health state HS_i , and within which T_{ij} sets are classified into the health state HS_j by the MD classifier, where $i, j = 1, 2, \dots, N_{HS}$, the element P_{ij} in the PoD matrix can be approximately calculated based on the definition as

$$T_{ij} = \begin{bmatrix} 86 & 0 & 14 \\ 0 & 98 & 2 \\ 9 & 3 & 88 \end{bmatrix} \quad (16)$$

$$P_{ij} \approx \frac{T_{ij}}{\sum_j T_{ij}} = \begin{bmatrix} 0.86 & 0.00 & 0.14 \\ 0.00 & 0.98 & 0.02 \\ 0.09 & 0.03 & 0.88 \end{bmatrix} \quad (17)$$

Since any set of testing data from the health state HS_i will definitely be classified into one of the predefined N_{HS} health states, the following equation regarding P_{ij} can be obtained:

$$\sum_{j=1}^{N_{HS}} P_{ij} = 1 \quad (18)$$

The above Eq. (18) suggests that the summation of each row in the PoD matrix will always equal to one. Similarly, the detectability, diagonal terms in the PoD matrix, for the health state HS_i can be obtained as

$$D_i = P_{ii} \approx [0.86 \quad 0.98 \quad 0.88] \quad (19)$$

4. Reliability based robust design optimization for structural sensing function design

Reliability-based robust design optimization (RBRDO) aims to find the best compromise between cost and reliability by taking uncertainties into account. Moreover, it can be used to ensure the robustness of system designs by minimizing design cost and its uncertainty factors while meeting system reliability or detectability requirements. In this study, the design of a smart sensing system is formulated with RBRDO to optimally allocate PZT sensors so that the robustness of the sensing system performance can be ensured and the detectability requirements for different failure modes can be guaranteed. Generally, the RBRDO formulation of the PZT sensing system design can be presented as an optimization problem as follows:

$$\begin{aligned} & \text{Minimize} && \sum_{j=1}^{nf} \mathbf{M}_j(\mathbf{x}, \mathbf{d}) + Q_f(\mathbf{x}, \mathbf{d}) \\ & \text{subject to} && D_i(\mathbf{x}, \mathbf{d}) \geq D_T, \quad i = 1 \dots n \\ & && \mathbf{x}^L \leq \mathbf{x} \leq \mathbf{x}^U, \quad \mathbf{x} \in R^{nr} \\ & && \mathbf{d}^L \leq \mathbf{d} \leq \mathbf{d}^U, \quad \mathbf{d} \in R^{nd} \end{aligned} \quad (20)$$

where the design constraints involved in the sensing systems design framework are detectability requirements considering uncertainties introduced by PZT material properties, manufacturing processes, as well as operating conditions. The design variables are the decision variables for PZT sensors dimension, PZT sensors locations, and the parameters for controlling the sensing process. The intent of the sensing systems design optimization is to minimize the cost while ensuring the design robustness and satisfying all detectability requirements. The objective function is thus defined as minimizing PZT sensor size and its variance, where $\mathbf{M}(\mathbf{x}, \mathbf{d})$ is the material and installation cost of PZT sensors for a given sensing system design, $Q_f(\mathbf{x}; \mathbf{d})$ is robustness penalty cost associated with the quality loss, which is measured by the variability of the cost function \mathbf{M} , D_i is the detectability of the sensing system for the HS_i , D_T is the target detectability, \mathbf{x}^U and \mathbf{x}^L are upper and lower bounds for the random design variables \mathbf{x} , respectively, whereas \mathbf{d}^U and \mathbf{d}^L are upper and lower bounds for the deterministic design variables \mathbf{d} . The parameters n , n_r , and n_f are the numbers of probabilistic constraints, random variables, design variables, and objective functions, respectively.

The RBRDO problem in Eq. (20) contains discrete decision variables for the selection of sensing devices, integer variables for the

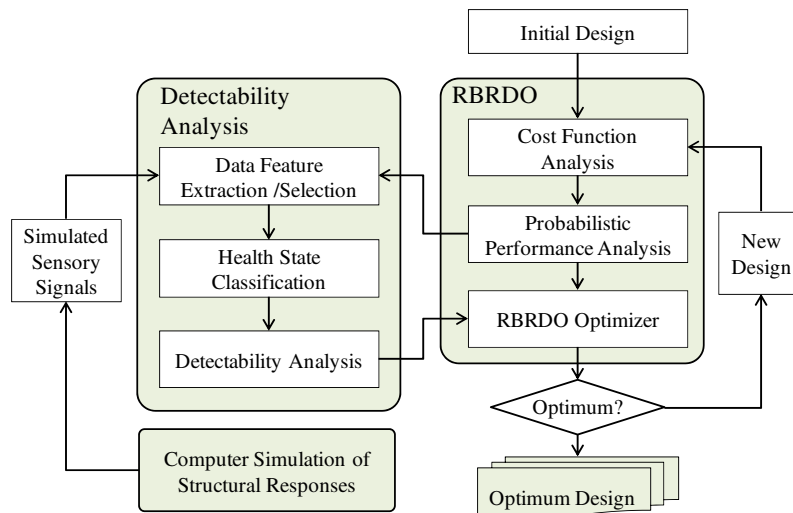


Fig. 3. RBRDO flowchart for detectability-based sensing function design.

number of selected sensing devices, as well as continuous variables for the sensor locations. Thus, it is formulated as a mixed-integer nonlinear programming (MINLP) problem [54], and heuristic algorithms such as Genetic Algorithms (GAs) can be used as the optimizer for the optimization purpose. In this study, the GA is employed for the example problem that will be detailed in the subsequent section. More alternative algorithms for solving the MINLP problem can be found in the references [54,56]. Fig. 3 shows the flowchart of the SN design optimization process. As shown in the figure, the process starts from an initial design and goes into the design optimization subroutine (the right hand side grey box), which will carry out the sensing function design cost analysis, call the detectability analysis subroutine (the left hand side grey box) to evaluate the performance of the sensing function at the current design, and execute the optimizer to generate the new designs if the optimality condition is not met. In the detectability analysis subroutine, the detectability analysis as discussed in the previous section will be carried out. Before solving the optimization problem, valid system computer simulation models have to be built and structural simulations have to be accomplished so that the training and testing data sets for each predefined health state are available at the iterative design optimization process for detectability analysis.

5. Case studies

In this section, the developed reliability-based robust design optimization technique for smart sensing function design using piezoelectric materials is demonstrated with two design case studies. In the first case study, the sensing function will be design for a rectangular aircraft wing panel considering rivet joint failures, whereas the second case study designs smart sensing function for power transformer mechanical fault diagnosis. The rest of this section details the two design case studies and results using the developed RBRDO sensing function design methodology.

5.1. Sensing function design for a rectangular aircraft wing panel

This subsection demonstrates the proposed RBRDO approach by designing PZT material based sensor patches for a rectangular aircraft wing panel. As shown in Figs. 4 and 5, the aircraft wing panel considered in this study has dimensions of two meters by one meter and is fastened by eight rivet joints, as indicated by L₁–L₈, respectively. There is a harmonic force *F* with a frequency of 120 Hz applied in the middle of panel to detect joint failures. In this case study, eight health states are defined based on the different rivet joint failure and combinations, as listed in Table 3. To identify the healthy state of the panel, four square PZT sensors are attached to the surface of panel. The electrical potential signal, obtained out of the PZT sensors, is used to identify the health state based on Mahalanobis distance.

The objective function of this RBRDO is to minimize PZT sensor size and its variance while the detectability of each health state meets its requirement to be greater than the target 0.99. For each sensor, the coordinate and side length of each squared PZT sensor are chosen as design variables, thus totally there are 12 design variables for this case study. All the design variables are assumed to be normal distributed and their upper and lower bounds of means and standard deviation are shown in Table 4. Besides the random design variables, three geometric random parameters are also considered in this case study, as listed in Table 5.

In this case study, RBRDO of sensing system for the rectangular panel can be formulated as follows:

$$\begin{aligned}
 & \text{Minimize} && \sum_{j=1}^4 S_j + \text{Var} \left(\sum_{j=1}^4 S_j \right) \\
 & \text{subject to :} && D_i(X, Y, S) \geq D_T, \quad i = 0 \dots 7 \\
 & && x^L \leq x \leq x^U, \quad X \in R^{nr} \\
 & && y^L \leq y \leq y^U, \quad Y \in R^{nr} \\
 & && s^L \leq s \leq s^U, \quad S \in R^{nr}
 \end{aligned} \tag{21}$$

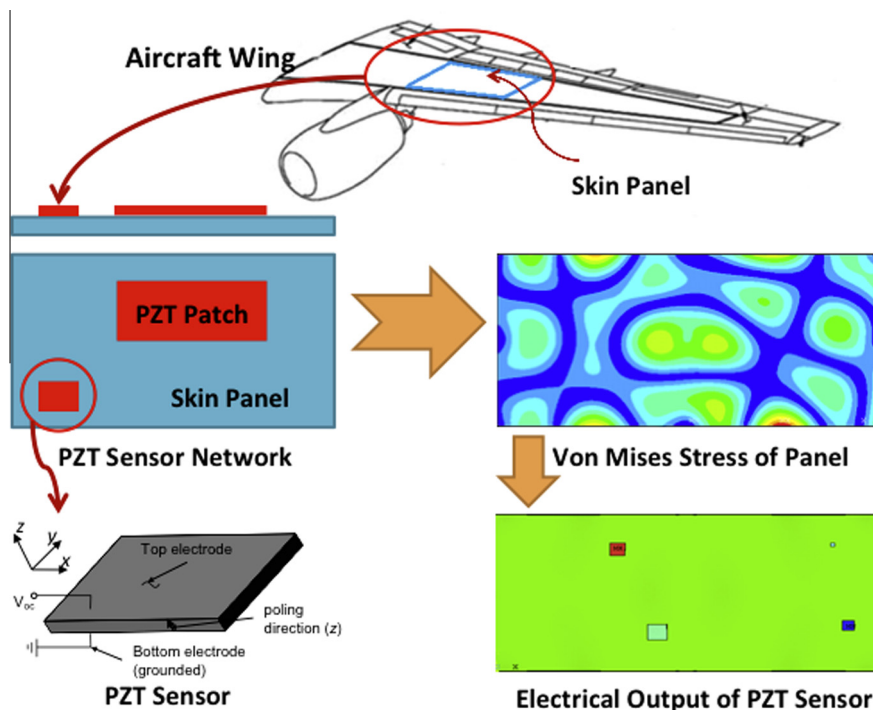


Fig. 4. Sensing function design of an aircraft wing panel using piezoelectric materials.

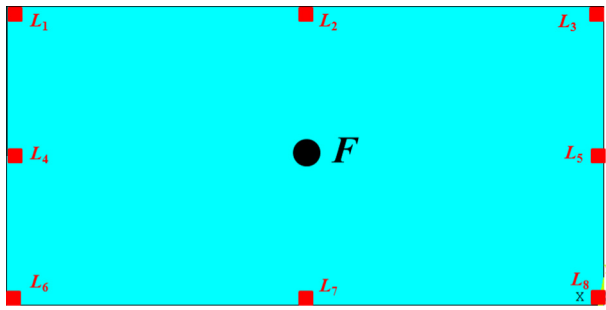


Fig. 5. Rectangular aircraft wing panel with indicated rivet joints.

Table 3 Health states definition of aircraft wing panel case study.

Health states	HS_0	HS_1	HS_2	HS_3	HS_4	HS_5	HS_6	HS_7
Joint failure	None	L_6	L_7	L_4	L_6, L_7	L_6, L_4	L_4, L_7	L_4, L_6, L_7

Table 4 Design variables of the rectangular aircraft wing panel case study.

Variables	Definition	LB	UB	Distribution	SD
X_1	X coordinate of the first sensor	0	2	Normal	0.02
Y_1	Y coordinate of the first sensor	0	1	Normal	0.02
S_1	Side length of the first sensor	0	0.1	Normal	$2e-3$
X_2	X coordinate of the second sensor	0	2	Normal	0.02
Y_2	Y coordinate of the second sensor	0	1	Normal	0.02
S_2	Side length of the second sensor	0	0.1	Normal	$2e-3$
X_3	X coordinate of the third sensor	0	2	Normal	0.02
Y_3	Y coordinate of the third sensor	0	1	Normal	0.02
S_3	Side length of the third sensor	0	0.1	Normal	$2e-3$
X_4	X coordinate of the fourth sensor	0	2	Normal	0.02
Y_4	Y coordinate of the fourth sensor	0	1	Normal	0.02
S_4	Side length of the fourth sensor	0	0.1	Normal	$2e-3$

Table 5 Random parameters of the rectangular aircraft wing panel case study.

Parameters	Definition	Distribution	Mean	SD
L	Length of panel	Normal	10	0.1
W	Width of panel	Normal	5	0.05
F	Amplitude of force	Normal	1000	50

where the objective function is to minimize the total area of PZT sensors and its variance, as denoted by the summation of the area S_j for each sensor unit. The detectability target is set as 0.99 for all seven health states. To obtain the electrical potential response of PZT attached on the panel, a 3D finite element model is established in ANSYS 12. Fig. 6 shows a particular sensor layout and its vibration displacement of health states HS_0 . The electrical potential contours of four PZT sensors are shown in Fig. 7.

The location and size of PZT sensor can directly determine the electrical potential response given a certain scenario. In this case, sensor S_2 and S_3 get relative significant electrical response while there is almost no obvious electrical potential for sensor S_1 and S_4 . Due to the uncertainties involved from not only the whole structural but also the sensing system, the signal output of each sensor is also a random value. Generic algorithm is used to search optimal solution for the RBRDO problem, and the optimal design is

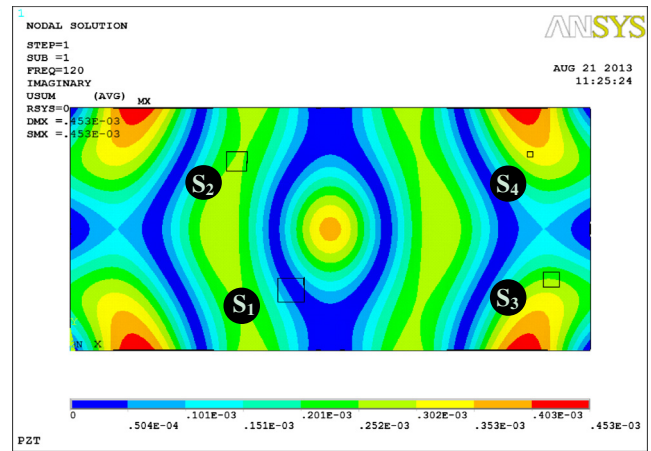


Fig. 6. Sensor layout and vibration amplitude contour of the panel for HS_0 .

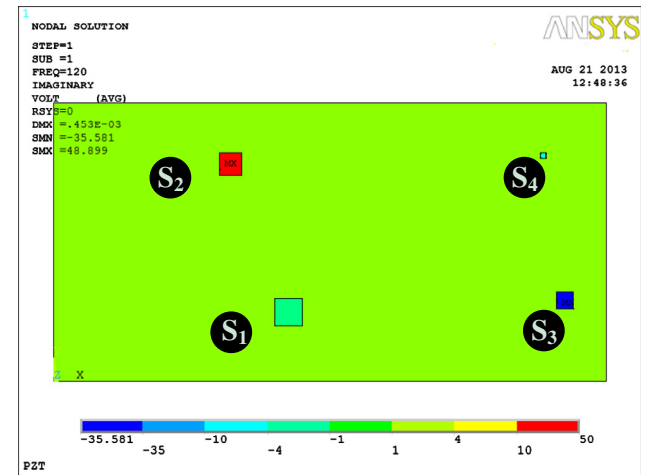


Fig. 7. Electrical potential contours of four PZT sensors.

obtained after 15 generations. The design history is shown in Table 6 while the corresponding detectability and cost are shown in Table 7 in which C_T represents the total cost comprising design cost M and quality lost Q_c . The corresponding detectability of each generation is also shown in Fig. 8. Fig. 9 demonstrates the cost distribution of initial and optimum designs while Fig. 10 shows the optimum layout of sensor system. As shown in the Fig. 9; both the mean and variance of design cost are increased slightly while the detectability of sensing system is improved significantly.

5.2. Sensing function design for power transformer mechanical fault diagnostics

Power transformers are among the most expensive elements of high-voltage power systems. The monitoring of power transformers enables the transition from the traditional time-based maintenance to the condition-based maintenance, resulting in significant reductions in maintenance costs. Due to the difficulties of direct measurement inside the transformer, the data that are actually most often used for both diagnosis and prognosis of transformers are obtained through indirect measurements. For example, measurements of temperature are firstly accomplished at accessible points and a modeling of the gradient can then be used to induce the maximum temperature in some areas; electric parameters and analysis of moisture content of the cooling oil are often performed for the diagnosis and condition-based maintenance of

Table 6
Iterative design history of rbrdo for the aircraft wing panel case study.

Iter.	X_1	Y_1	S_1	X_2	Y_2	S_2	X_3	Y_3	S_3	X_4	Y_4	S_4
1	12.00	12.00	3.00	110.00	60.00	3.00	12.00	60.00	3.00	110.00	12.00	3.00
2	23.64	17.87	3.80	175.64	71.10	3.20	18.52	65.55	6.79	175.70	61.45	5.77
3	71.91	27.42	5.11	115.07	71.65	3.44	68.83	64.02	6.07	139.60	67.59	3.03
4	71.91	25.34	3.45	115.07	77.63	3.44	68.83	64.02	6.07	168.58	69.27	3.03
5	71.91	25.34	3.45	115.07	77.63	3.44	68.83	64.02	6.07	139.60	69.27	3.03
6	73.91	25.34	3.45	115.07	77.63	3.44	68.83	64.02	4.07	141.60	69.27	3.03
7	75.91	25.34	3.45	115.07	77.63	3.44	68.83	64.02	4.07	141.60	69.27	3.03
8	75.91	25.34	3.45	167.15	77.63	3.00	68.83	60.31	4.07	141.60	69.27	3.03
9	75.91	25.34	3.45	167.15	77.63	3.00	68.83	60.31	4.07	141.60	69.27	3.03
10	73.91	25.34	3.45	115.07	77.63	3.00	68.83	60.31	4.07	141.60	69.27	3.03
11	73.91	25.34	3.45	115.07	77.63	3.00	68.83	60.31	4.07	142.60	69.27	3.03
12	76.91	25.34	3.45	115.07	79.35	3.00	68.83	60.31	3.07	142.60	69.27	3.03
13	76.91	25.34	3.45	115.07	79.35	3.00	68.83	60.31	3.07	142.60	69.27	3.03
14	76.91	25.34	3.45	115.07	79.35	3.00	68.83	60.31	3.07	142.60	69.27	3.03
15	76.91	25.34	3.45	115.07	79.35	3.00	68.83	60.31	3.07	142.60	69.27	3.03

Table 7
Detectability and cost of RBRDO for the aircraft wing panel case study.

Iter.	D_0	D_1	D_2	D_3	D_4	D_5	D_6	D_7	M	Q_c	CT
1	0.79	0.96	0.93	0.95	0.90	0.97	0.94	0.95	36.00	5.76	41.76
2	0.96	1.00	0.98	0.98	1.00	1.00	0.99	1.00	104.0	16.70	120.7
3	0.97	0.99	0.97	0.99	1.00	1.00	1.00	0.99	84.00	13.45	97.45
4	0.98	0.98	1.00	0.99	0.99	1.00	1.00	0.98	69.76	11.10	80.86
5	0.99	1.00	1.00	1.00	1.00	1.00	1.00	0.99	69.76	11.21	80.97
6	0.99	1.00	1.00	1.00	1.00	1.00	1.00	0.99	49.48	7.91	57.39
7	0.99	1.00	1.00	1.00	1.00	1.00	1.00	0.99	49.48	7.93	57.41
8	0.98	0.99	1.00	0.99	1.00	1.00	1.00	1.00	46.62	7.47	54.09
9	0.98	0.99	1.00	0.99	1.00	1.00	1.00	1.00	46.62	7.49	54.11
10	0.98	0.99	1.00	0.99	1.00	1.00	1.00	0.99	46.62	7.44	54.06
11	0.98	0.99	1.00	0.99	1.00	1.00	1.00	0.99	46.62	7.50	54.12
12	0.99	0.99	1.00	1.00	1.00	0.99	1.00	1.00	39.48	6.35	45.83
13	0.99	0.99	1.00	1.00	1.00	0.99	1.00	1.00	39.48	6.31	45.79
14	0.99	0.99	1.00	1.00	1.00	0.99	1.00	1.00	39.48	6.29	45.77
15	0.99	0.99	1.00	1.00	1.00	0.99	1.00	1.00	39.48	6.33	45.81

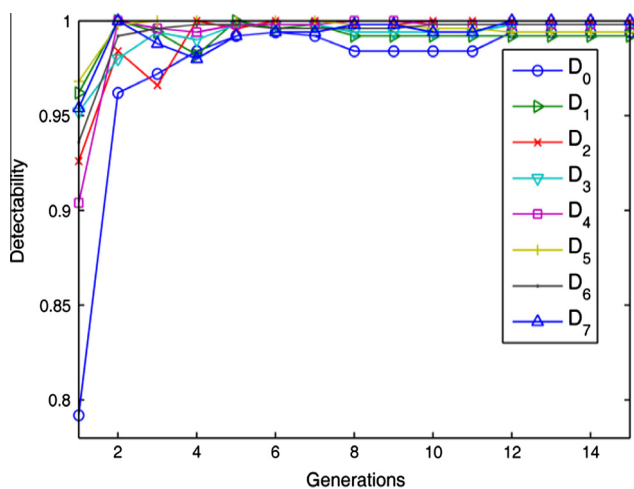


Fig. 8. The detectability history of RBRDO for the aircraft wing panel case study.

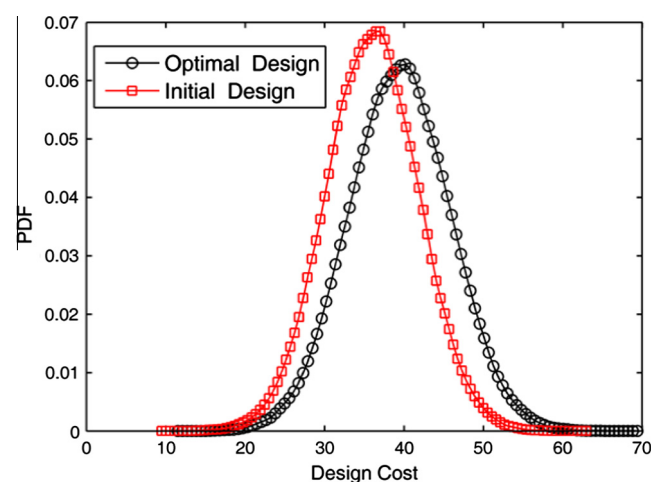


Fig. 9. The cost distributions of initial and optimal design.

transformers, with frequency response analysis of electric characteristics being common; the vibrations of the magnetic core and of the windings could characterize transitory overloads and permanent failures before any irreparable damage occurs. This case study aims at designing an optimum PZT sensor system on the front wall surface of a power transformer. The measurements of the transformer vibration responses induced by the magnetic field loading enables the detection of mechanical failures of winding support joints inside the transformer.

In this study, the winding support joint loosening is considered as the failure mode, the detection of which will be realized by collecting the vibration signal, induced by the magnetic field loading with a fixed frequency on the power transformer core, using the optimally designed PZT sensor system at the external surface of the transformer. The validated finite element (FE) model of a power transformer was created in ANSYS as shown in Fig. 11, where one exterior wall is concealed to make the interior structure visible. Fig. 12 shows 12 simplified winding support joints with 4

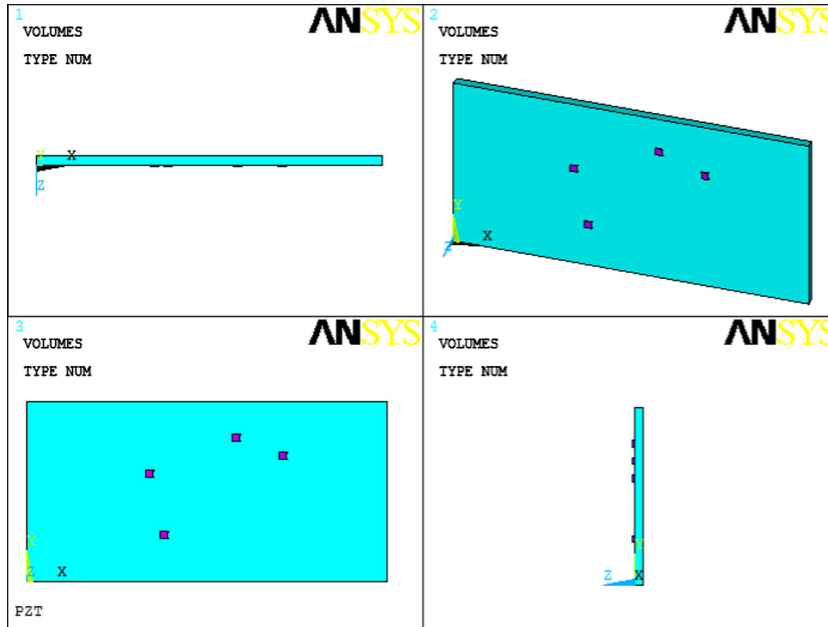


Fig. 10. Layout of the Sensors for the Optimum Design.

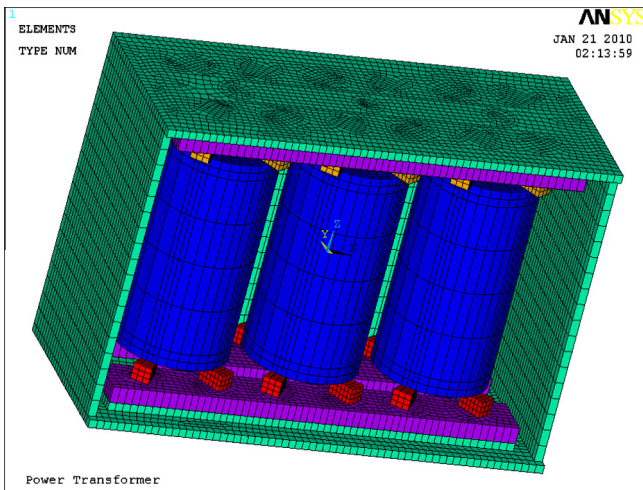


Fig. 11. A power transformer FE model (without the covering wall).

for each winding. The transformer is fixed at the bottom surface and a vibration load with the frequency of 120 Hz is applied to the transformer core. The joint loosening has been realized by reducing the stiffness of the joint itself. Different combinations of the loosening joints will be treated as different health states of the power transformer which will be detailed in the next subsection. The uncertainties in this case study are modeled as random parameters with corresponding statistical distributions listed in Table 8. These uncertainties will be propagated into the structural vibration responses and will be accounted for when designing an optimum PZT sensor system.

For the purpose of demonstrating the proposed design methodology, 9 representative health states shown in Table 9 were selected from all possible combinations of 12 winding support joint failures. Among these 9 selected health states, HS_1 denotes the healthy condition without any loosening joint, whereas HS_2 – HS_9 are health states with either one or two loosening joints. According to the statistical properties of random parameters in Table 8 and 200 sets of random samples were generated and the

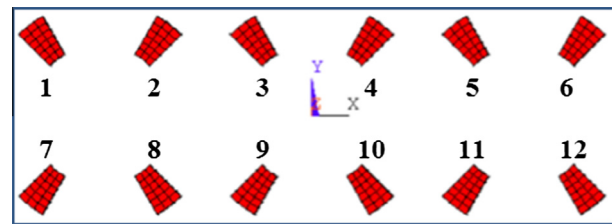


Fig. 12. Winding support joints and their numberings.

Table 8
Random property of the power transformer.

Random variable	Randomness (cm, g, degree)
Young's modulus of support joint	$N(2e12, 4e10^2)$
Young's modulus of loosening joints	$N(2e10, 4e8^2)$
Young's modulus of winding	$N(1.28e12, 3e10^2)$
Poisson ratio of joints	$N(0.27, 0.0054^2)$
Poisson ratio of winding	$N(0.34, 0.0068^2)$
Density of joints	$N(7.85, 0.157^2)$
Density of windings	$N(8.96, 0.179^2)$
Length of PZT layer	$N(S, (0.05 * S)^2)$

Table 9
Definition of system health states.

Health state	1	2	3	4	5	6	7	8	9
Loosening joints	–	1	2	3	1, 2	1, 3	1, 5	1, 9	1, 11

simulations for each of 9 health states were carried out and the average electrical potentials of PZT layers were extracted as sensor signals and saved as the simulation results.

The displacement contour of the healthy state power transformer at the nominal values of the random parameters from the structural simulation is shown in Fig. 13.

Similar to the first case study, applying the developed sensor network design methodology for the power transformer case study, the design problem can be formulated as follows:

$$\begin{aligned}
 & \text{Minimize} \quad \sum_{j=1}^4 S_j + \text{Var} \left(\sum_{j=1}^4 S_j \right) \\
 & \text{subject to:} \quad D_i(X, Y, S) \geq D_T, \quad i = 1 \dots 9 \\
 & \quad \quad \quad x^L \leq x \leq x^U, \quad X \in R^{nr} \\
 & \quad \quad \quad y^L \leq y \leq y^U, \quad Y \in R^{nr} \\
 & \quad \quad \quad s^L \leq s \leq s^U, \quad S \in R^{nr}
 \end{aligned}
 \tag{22}$$

where the objective function is to minimize the total area of PZT sensors and its variance, and the detectability target has been set to 0.90 for all nine health states. To conduct the design optimization of the piezoelectric material based sensor network, the simulation has been conducted with random inputs as given in Table 8. The first 100 sets of simulation results were used as the training data set and the others were used as testing data set. These simulation results were later used to evaluate the detectability of sensor system. As mentioned in the previous section, this case study problem is formulated as designing a PZT sensor system on the surface of the covering wall of the power transformer to minimize the cost of the SN while satisfying the detectability constraints for each health state, i.e., the detectability should be greater than a target detectability of 0.9. In the RBRDO framework, the cost function is defined as the sum of two parts: the mean and variance of total PZT area; the total number of PZT sensor are four and the PZT sensors are assumed to be square. The design variables in this case study include: (1) location of each PZT sensor, (2) length of each PZT sensor. The RBRDO problem in this case study was solved using the genetic algorithm. With the target detectability being 0.9, we obtained the optimum sensor system design on the outer wall surface (140 cm × 90 cm) with totally 4 sensors, as shown in

Table 10. Figs. 14 and 15 show the detectability and cost history of RBRDO process for 9 health states, respectively, whereas Fig. 16 demonstrates the distribution of initial and optimum sensor system designs. The final optimum sensor system is illustrated in Fig. 17.

5.3. Remarks on the case studies

This subsection provides the remarks of the two case studies as presented in the previous two subsections.

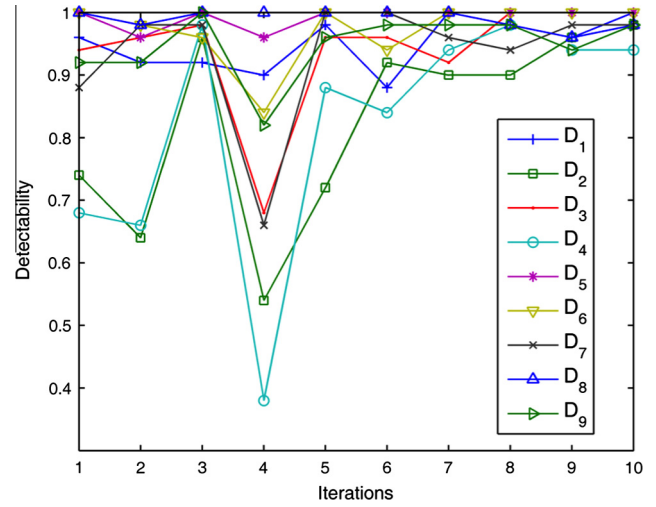


Fig. 14. Detectability history during RBRDO.

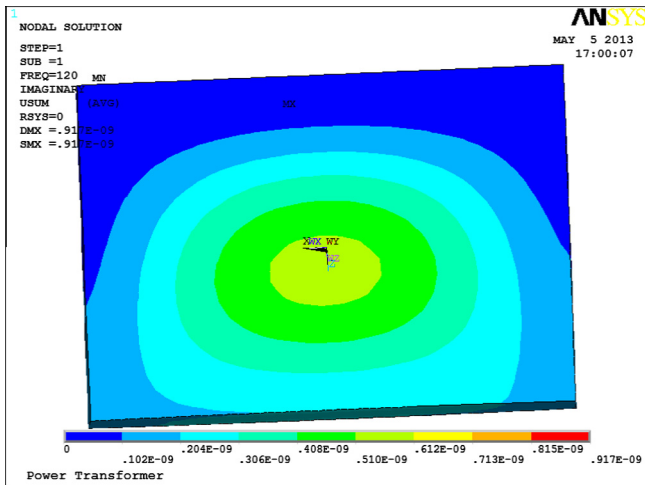


Fig. 13. Vibration contour of the winding support for the healthy state of power transformer.

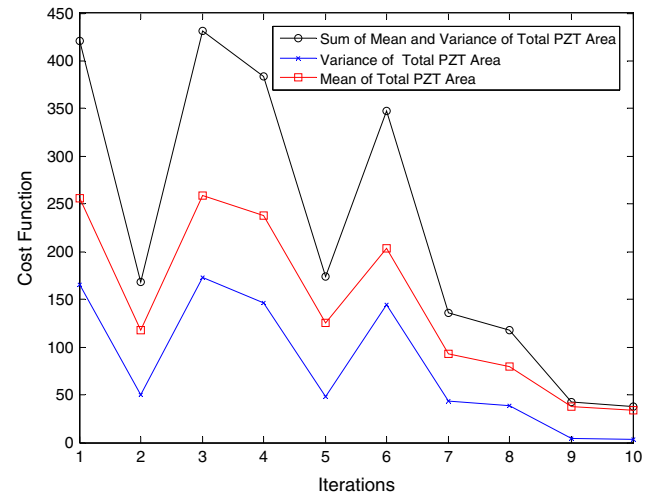


Fig. 15. Cost history during RBRDO.

Table 10 Design history during RBRDO.

Iter.	X_1	Y_1	S_1	X_2	Y_2	S_2	X_3	Y_3	S_3	X_4	Y_4	S_4
1	-40.00	-35.00	8.00	-40.00	20.00	8.00	40.00	-35.00	8.00	40.00	45.00	8.00
2	-36.87	-15.35	4.93	-32.03	0.22	1.50	0.80	-23.61	5.71	0.67	0.84	7.68
3	-40.00	-35.00	8.00	-21.56	0.26	8.00	40.00	-35.00	8.86	40.00	0.25	7.22
4	-14.87	-22.73	7.66	-56.55	20.00	8.00	0.41	-35.00	8.00	0.91	0.22	7.16
5	-46.05	-35.00	1.82	-40.00	0.83	6.37	0.44	-35.00	6.60	0.95	0.05	6.17
6	-52.32	-34.00	1.82	-12.50	0.13	9.00	40.00	-35.00	6.30	0.95	0.16	8.91
7	-71.74	-35.00	8.00	-40.00	0.13	3.96	0.14	-54.12	2.19	40.00	0.27	2.88
8	-46.05	-35.00	3.19	-40.00	0.26	7.81	40.00	-35.00	2.19	40.00	0.27	1.88
9	-46.05	-35.00	3.19	-40.00	0.26	3.82	40.00	-43.45	2.19	40.00	0.27	2.88
10	-71.74	-35.00	2.51	-40.00	0.13	3.82	40.00	-43.45	2.19	40.00	0.96	2.88

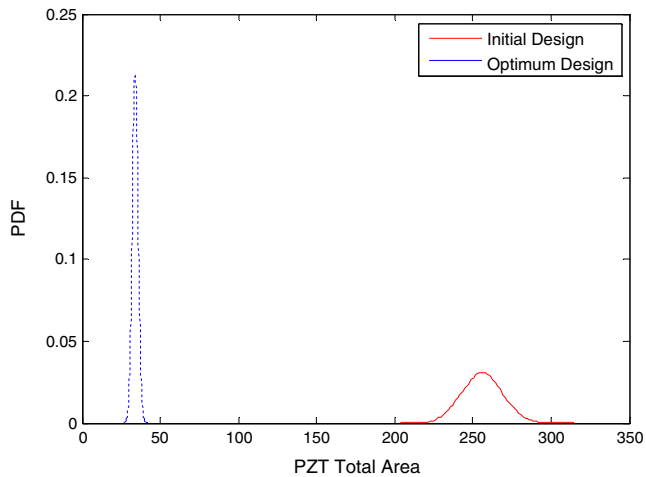


Fig. 16. Cost distribution of initial and optimum designs.

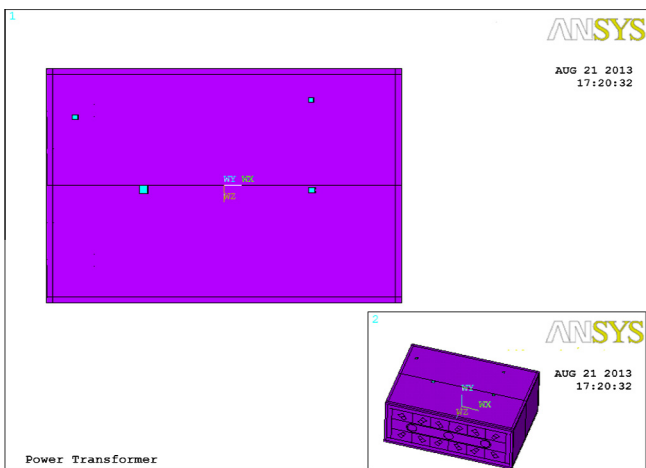


Fig. 17. Optimal layout of sensor system.

Remark 1. In this study, the detectability of the designed sensor networks using piezoelectric materials has been calculated based on finite element simulation models. Note that the simulation model is an important factor that would affect the results of sensor network designs. In the previous study, the experimental validation for the structure simulation models coupled with piezoelectric materials has been performed and reported in one of the authors' previous publications [57], where an excellent agreement of open circuit voltage between the simulation and the test has been reported. In the studies presented in this paper, the same modeling and simulation strategies as reported in [57] have been used. As this study is focused on developing a new probabilistic design framework based on the new detectability concept for generic smart sensing systems, the authors assumed that the simulation models used in both case studies are valid.

Remark 2. In the power transformer case study, the electrical field inside the power transformer could have an impact on the piezoelectric sensors attached to it. However, it is assumed that the impact of electric field inside the power transformer windings on piezoelectric sensor outputs is minor compared to the one contributed by power transformer vibrations. Thus, to maintain the case study in a certain level of simplicity without losing the generosity to demonstrate the proposed sensor network design methodology, the internal electric field impact has been neglected in this study.

6. Conclusion

This paper presented a reliability-based robust design optimization approach for the development of piezoelectric materials based structural sensing systems for failure diagnostics and prognostics, to ensure the robustness of sensing performance. In the proposed approach, a detectability measure is defined to evaluate the performance of any given sensing system, and the sensing system design problem can be formulated to maximize detectability for different failure modes by optimally allocating piezoelectric materials into a target structure. This formulation can be conveniently solved within a reliability-based robust design framework to ensure design robustness while considering the uncertainties. Two case studies were employed to demonstrate the effectiveness of the proposed methodology in developing multifunctional material sensing systems. The case study results indicated that the developed approach is very effective for the structural sensing design problems considering the uncertainties, in that it takes into account the performance variability in the design optimization process thus the design cost can be reduced while simultaneously the performance robustness can be ensured and all detectability requirements can be satisfied.

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Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.compstruc.2015.04.012>.

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